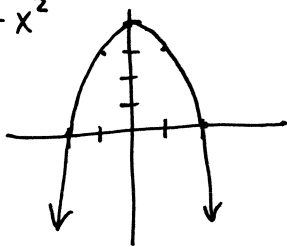


Section 1.2 : 5-49 odd, 51-55 odd, 65-70 all, 72

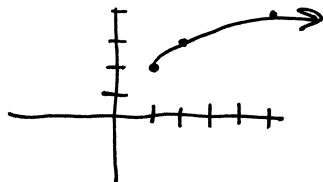
5. $y = 4 - x^2$



$D: (-\infty, \infty)$

$R: (-\infty, 4]$

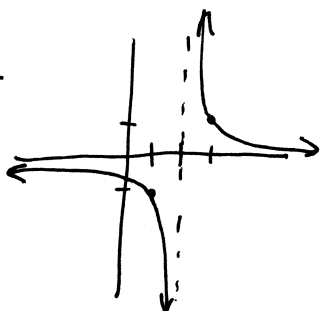
7. $y = \sqrt{x-1} + 2$



$D: [1, \infty)$

$R: [2, \infty)$

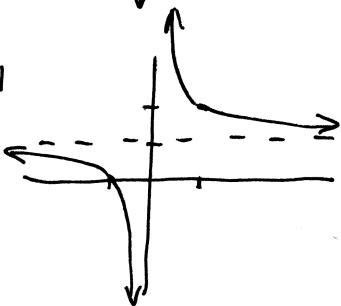
9. $y = \frac{1}{x-2}$



$D: (-\infty, 2) \cup (2, \infty)$

$R: (-\infty, 0) \cup (0, \infty)$

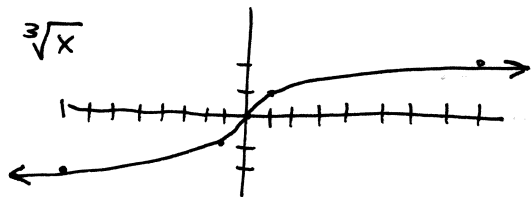
11. $y = \frac{1}{x} + 1$



$D: (-\infty, 0) \cup (0, \infty)$

$R: (-\infty, 1) \cup (1, \infty)$

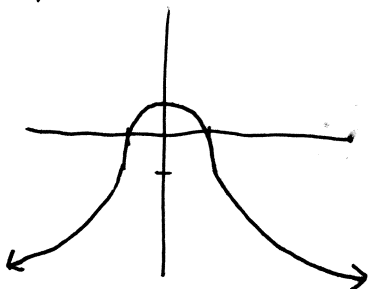
13. $y = \sqrt[3]{x}$



$D: (-\infty, \infty)$

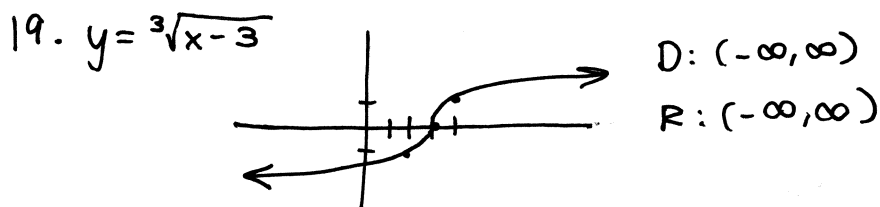
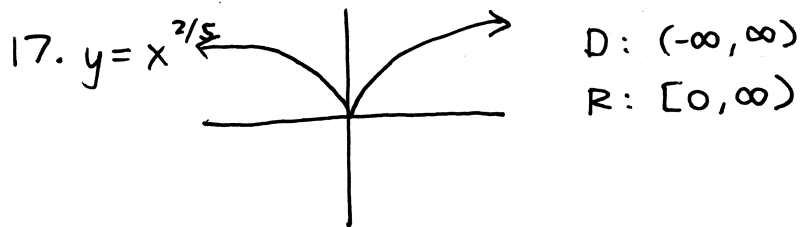
$R: (-\infty, \infty)$

15. $y = \sqrt[3]{1-x^2}$



$D: (-\infty, \infty)$

$R: (-\infty, 1]$



21. Even $(-x)^4 = x^4$

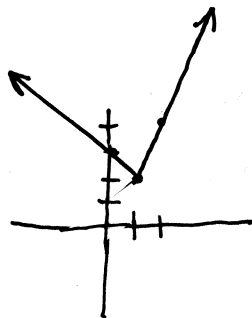
23. Neither $-x+2$

25. $\sqrt{(-x)^2+2} = \sqrt{x^2+2} \rightarrow$ Even

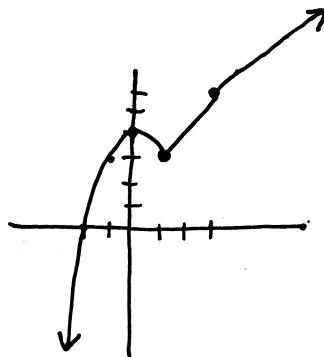
27. $\frac{(-x)^3}{(-x)^2-1} = \frac{-x^3}{x^2-1} = -\frac{x^3}{x^2-1} \rightarrow$ Odd

29. $\frac{1}{-x-1} \rightarrow$ Neither

31. $f(x) = \begin{cases} -x+3, & x \leq 1 \\ 2x, & x > 1 \end{cases}$



33. $f(x) = \begin{cases} 4-x^2, & x < 1 \\ 3/2x + 3/2, & 1 \leq x \leq 3 \\ x+3, & x > 3 \end{cases}$



35. Each x value has only one y value, which is the definition of a function.

37. No

39. Yes

41. $f(x) = \begin{cases} x, & 0 \leq x \leq 1 \\ -x+2, & 1 \leq x \leq 2 \end{cases}$

$$43. f(x) = \begin{cases} -x+2, & 0 < x \leq 2 \\ -\frac{1}{3}x + \frac{5}{3}, & 2 < x \leq 5 \end{cases}$$

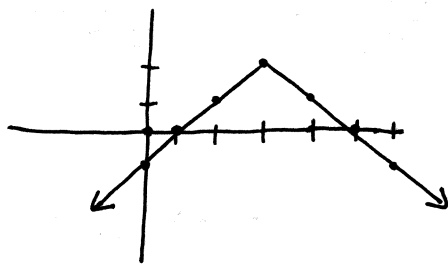
$$45. f(x) = \begin{cases} -x, & -1 \leq x < 0 \\ 1, & 0 < x \leq 1 \\ -\frac{1}{2}x + \frac{3}{2}, & 1 \leq x < 3 \end{cases}$$

$$47. f(x) = \begin{cases} 0, & 0 \leq x \leq \frac{T}{2} \\ \frac{2}{T}x - 1, & \frac{T}{2} \leq x \leq T \end{cases}$$

$$m = \frac{\Delta y}{\Delta x} = \frac{1}{\frac{1}{2}T} = \frac{2}{T}$$

$$49. f(x) = -1|3-x| + 2$$

x	y
1	0
2	1
3	2
4	1
5	0



$$D: (-\infty, \infty)$$

$$R: (-\infty, 2]$$

$$51. f(x) = x+5, g(x) = x^2 - 3$$

$$a) f(g(x)) = x^2 - 3 + 5 = x^2 + 2$$

$$b) g(f(x)) = (x+5)^2 - 3 = x^2 + 10x + 25 - 3 = x^2 + 10x + 22$$

$$c) f(g(0)) = f(-3) = 2$$

$$d) g(f(0)) = g(5) = 5^2 - 3 = 22$$

$$e) g(g(-2)) = g(1) = 1^2 - 3 = -2$$

$$f) f(f(x)) = x+5+5 = x+10$$

$$53. a) x^2$$

$$b) 1 + \frac{1}{a} = x$$

$$\frac{1}{a} = \frac{x-1}{1} \rightarrow a = \frac{1}{x-1}$$

$$c) \frac{1}{x} \text{ bc } \frac{1}{(1/x)} = \frac{x}{1} = x \checkmark$$

$$d) x^2 \text{ bc } (\sqrt{x})^2 = x \checkmark$$

$$55. a) C = 2\pi r - \underset{\substack{\uparrow \\ \text{cut out}}}{x} = 2\pi(4) - x = 8\pi - x$$

$$b) C = 2\pi r \\ 8\pi - x = 2\pi r \rightarrow r = \frac{8\pi - x}{2\pi} = 4 - \frac{x}{2\pi}$$

$$c) r^2 + h^2 = 4^2 \rightarrow h = \sqrt{16 - r^2} \\ r^2 = \left(\frac{8\pi - x}{2\pi}\right)^2 = \frac{(8\pi - x)^2}{4\pi^2} = \frac{64\pi^2 - 16\pi x + x^2}{4\pi^2} \\ h = \sqrt{\frac{16}{1} - r^2} = \sqrt{\frac{64\pi^2 - (64\pi^2 - 16\pi x + x^2)}{4\pi^2}} = \frac{\sqrt{16\pi x - x^2}}{2\pi}$$

$$d) V = \frac{1}{3}\pi r^2 h = \frac{\pi}{3} \cdot \frac{(8\pi - x)^2}{4\pi^2} \cdot \frac{\sqrt{16\pi x - x^2}}{2\pi} = \frac{(8\pi - x)^2 \sqrt{16\pi x - x^2}}{24\pi^2}$$

$$65. f(x) = x^2 - 3, g(x) = \sqrt{x+2}$$

$$b) f \circ g = \sqrt{x+2}^2 - 3 = x+2-3 = x-1 \quad \text{with } x \geq -2$$

$$g \circ f = \sqrt{x^2 - 3 + 2} = \sqrt{x^2 - 1}$$

$$a) D: [-2, \infty), R: [-3, \infty)$$

$f \circ g$

$$D: (-\infty, -1] \cup [1, \infty), R: [0, \infty)$$

$g \circ f$

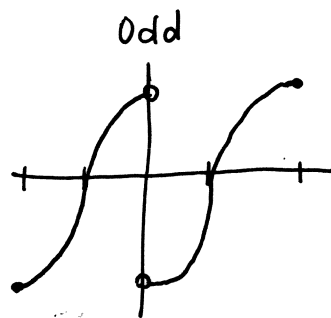
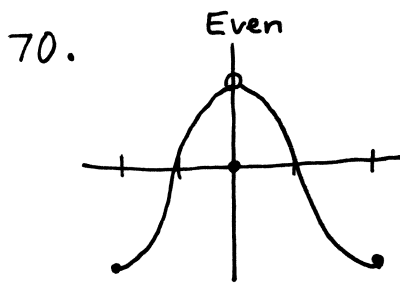
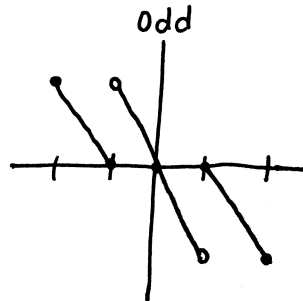
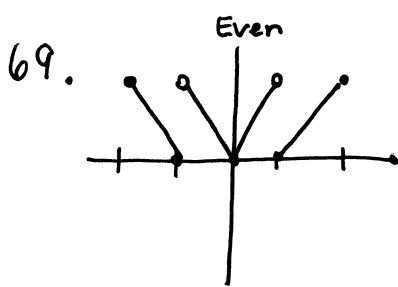
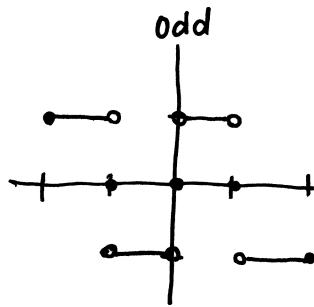
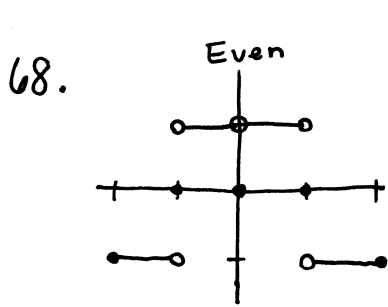
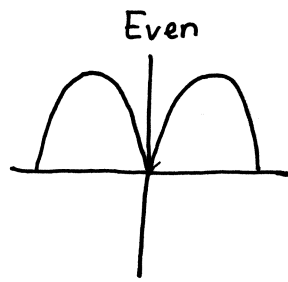
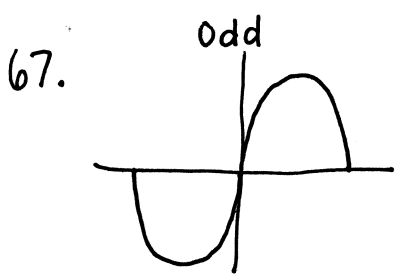
$$66. f(x) = \frac{2x-1}{x+3}, g(x) = \frac{3x+1}{2-x}$$

$$b) f \circ g = \frac{2\left(\frac{3x+1}{2-x}\right) - 1}{\frac{3x+1}{2-x} + 3} = \frac{\frac{6x+2}{2-x} - \frac{2-x}{2-x}}{\frac{3x+1}{2-x} + \frac{6-3x}{2-x}} = \frac{\frac{6x+2-2+x}{2-x}}{\frac{3x+1+6-3x}{2-x}} = \frac{\frac{7x}{2-x}}{\frac{7}{2-x}} = \frac{\cancel{7x}}{\cancel{2-x}} \cdot \frac{\cancel{2-x}}{\cancel{7}} = x \quad \text{with } x \neq 2$$

$$g \circ f = \frac{3\left(\frac{2x-1}{x+3}\right) + 1}{2 - \frac{2x-1}{x+3}} = \frac{\frac{6x-3}{x+3} + \frac{x+3}{x+3}}{\frac{2x+6}{x+3} - \frac{2x-1}{x+3}} = \frac{\frac{7x}{x+3}}{\frac{7}{x+3}} = \frac{\cancel{7x}}{\cancel{x+3}} \cdot \frac{\cancel{x+3}}{\cancel{7}} = x \quad \text{with } x \neq -3$$

$$a) f \circ g : D: (-\infty, 2) \cup (2, \infty), R: (-\infty, 2) \cup (2, \infty)$$

$$g \circ f : D: (-\infty, -3) \cup (-3, \infty), R: (-\infty, -3) \cup (-3, \infty)$$



72. a) Even: $f(-x) = f(x)$

$$f(-x) \cdot g(-x) = f(x) \cdot g(x) = f \cdot g(x)$$

Still even bc substituting $-x$ still produced the same result.

b) Odd: $f(-x) = -f(x)$

$$f(-x) \cdot g(-x) = -f(x) \cdot -g(x) = f(x) \cdot g(x) = f \cdot g(x)$$

Becomes even bc two negatives cancel and the result is positive.

5-1: Solving Equations Notes

*Ignore
this page.***Solve each equation.**

1) $a - 4 = -2$

2) $\frac{n}{3} = -4$

3) $72 = -6n + 6$

4) $9 = \frac{10 + n}{3}$

Solve each proportion.

5) $\frac{8}{10} = \frac{5}{x}$

Solve each equation.

6) $8m + 1 + 8m = -15$

7) $4(-6a + 1) = -164$

8) $8 - p = -7 + 2p$

Solve each equation for the indicated variable.

9) $u = a + k$, for a

10) $u = kx$, for x